

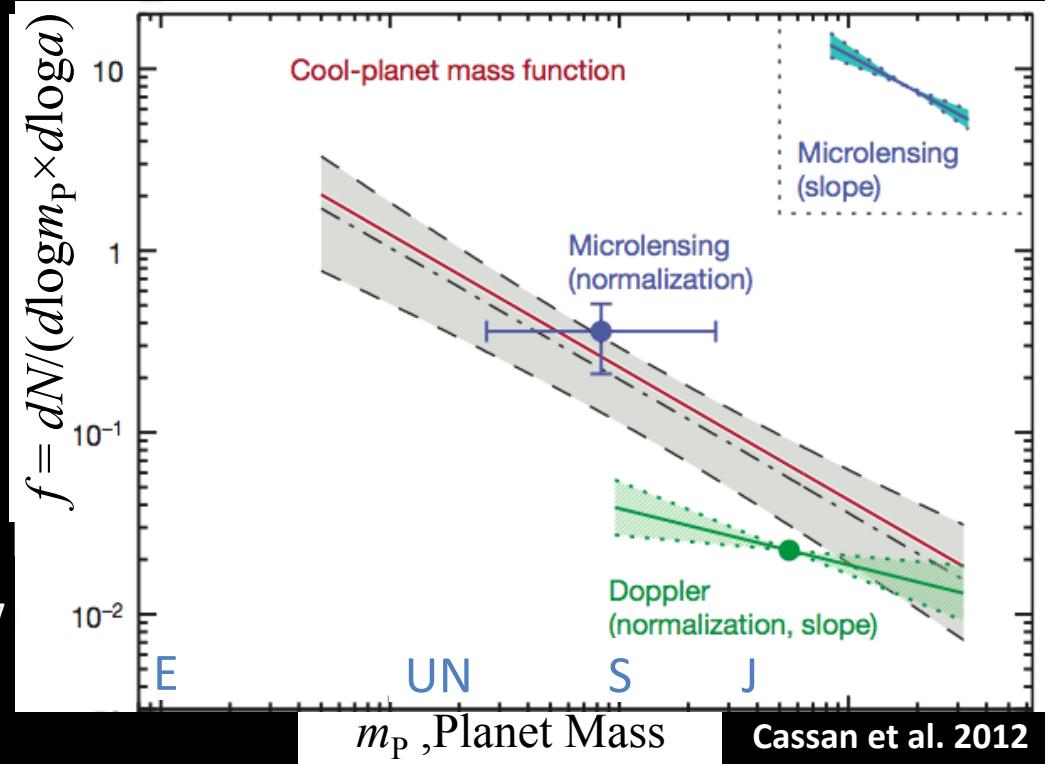
Planet Frequency with Mass Ratio, Separation and Event Time Scale

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Statistics from Microlensing

- Sumi et al. 2010
 - $f \propto q^{-0.68 \pm 0.2}$
- Gould et al. 2010
 - 0.36 ± 0.15 @ $q \sim 5 \times 10^{-4}$
- Cassan et al. 2012
 - $10^{-0.62 \pm 0.22} (M/M_{\text{Sat}})^{-0.73 \pm 0.17}$



This work: focus on planet frequencies with
 q : mass ratio
 s : separation
 t_E : event time scale
using MOA data in 2007-2012

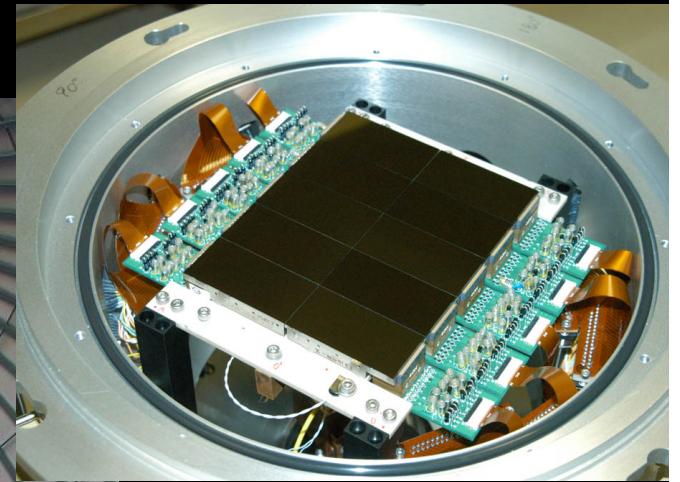
MOA

(since 1995)



(Microlensing Observations in Astrophysics)

(New Zealand/Mt. John Observatory, Latitude: 44°S, Alt: 1029m)

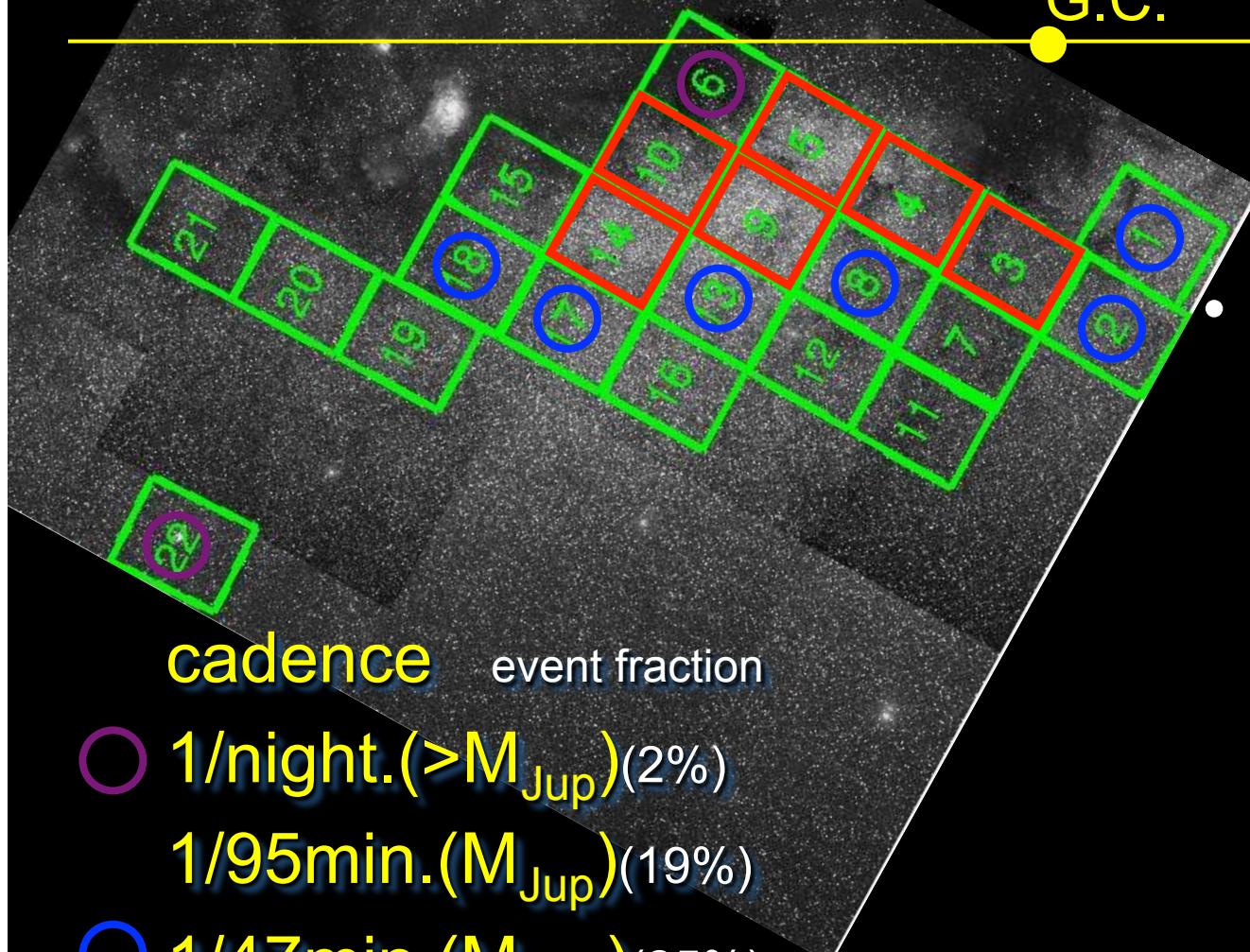


Mirror: 1.8m
CCD : 80M pix.
FOV : 2.2 deg.²
Filter : MOA-Red
(R + I)

Galactic Bulge Fields ($\sim 42 \text{ deg}^2$)



G.C.



cadence event fraction

○ 1/night. ($> M_{\text{Jup}}$) (2%)

1/95min. (M_{Jup}) (19%)

○ 1/47min. (M_{Nep}) (25%)

□ 1/15min. (M_{\oplus}) (54%)

- # of μ lens alerts
 - 2007: 488
 - 2008: 477
 - 2009: 563
 - 2010: 607
 - 2011: 485
 - 2012: 680
 - 2013: 668
 - 2014: 621

3300 events in 6 yrs

Event Selection

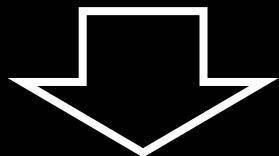
To construct a sample of well defined single and planetary events, we reject ...

1. Non-microlensing events (CVs, moving objects, ...)
2. Stellar binaries: $q > 0.03$
3. Events with insufficient data points

For, planetary events

Detection : MOA survey data

Characterization : All available data



Remaining events are 1316 events (from 3300 events/6yrs)
1291 single lens, 22 planetary, 3 ambiguous

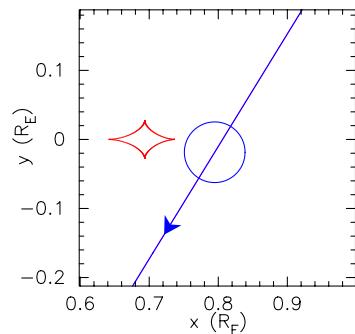
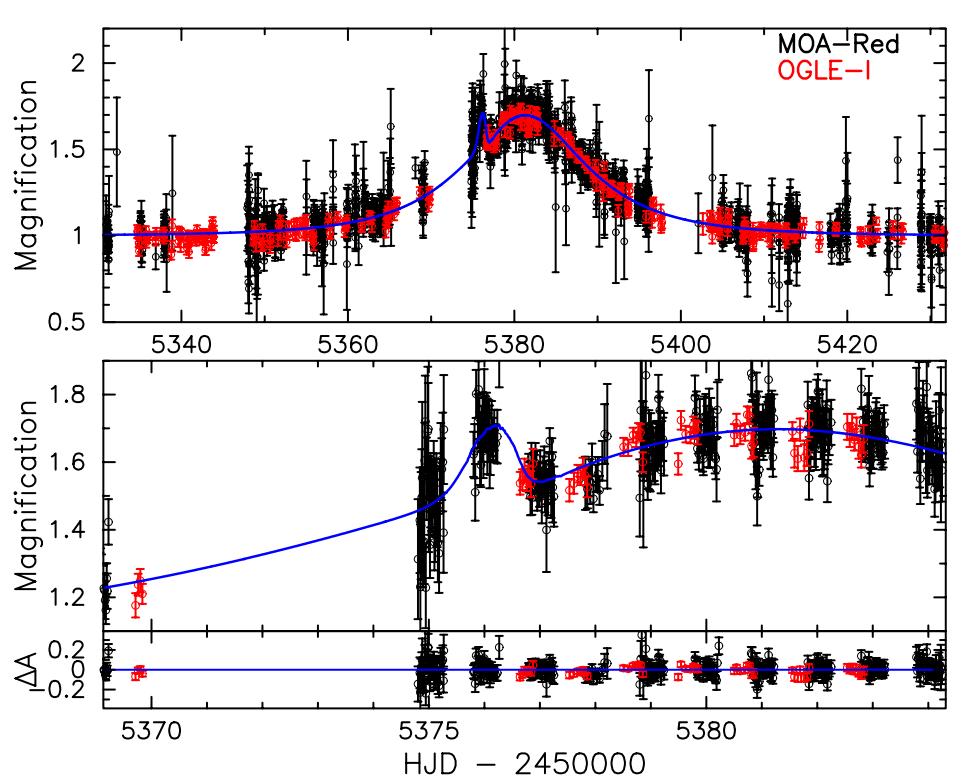
22 Planetary Events

Event	Paper	Event	Paper
MB07192	Bennett+2008	MB10477	Bachelet+2012
OB07368/MB07308	Sumi+2010	MB11028/OB110203	Skowron+ in prep.
OB07349/MB07379	Dong in prep.	OB110265/MB11197	Skowron+ 2014
OB08355/MB08288	Koshimoto+2014	MB11262/OB110703	Bennett+2014
MB08379	Suzuki+2014	MB11291	Bond+ in prep.
MB09266	Muraki+2011	MB11322/OB111127	Shvartzvald+2014
MB09319	Miyake+2011	MB12006/OB120022	
MB09387	Batista+2011	OB120563/MB12288	Fukui+ in prep.
MB10117	Bennett+ in prep.	MB12355	
MB10328	Furusawa+2013	MB12505	MOA in prep.
MB10353	Rattenbury+ in prep.	OB120950/MB12527	Koshimoto+ in prep.

4 planets found in the analysis of online data, 5 planets in 2012

New Planets in 22 Planetary Events

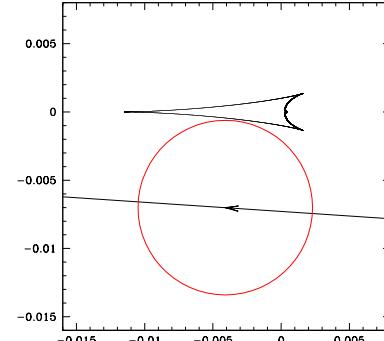
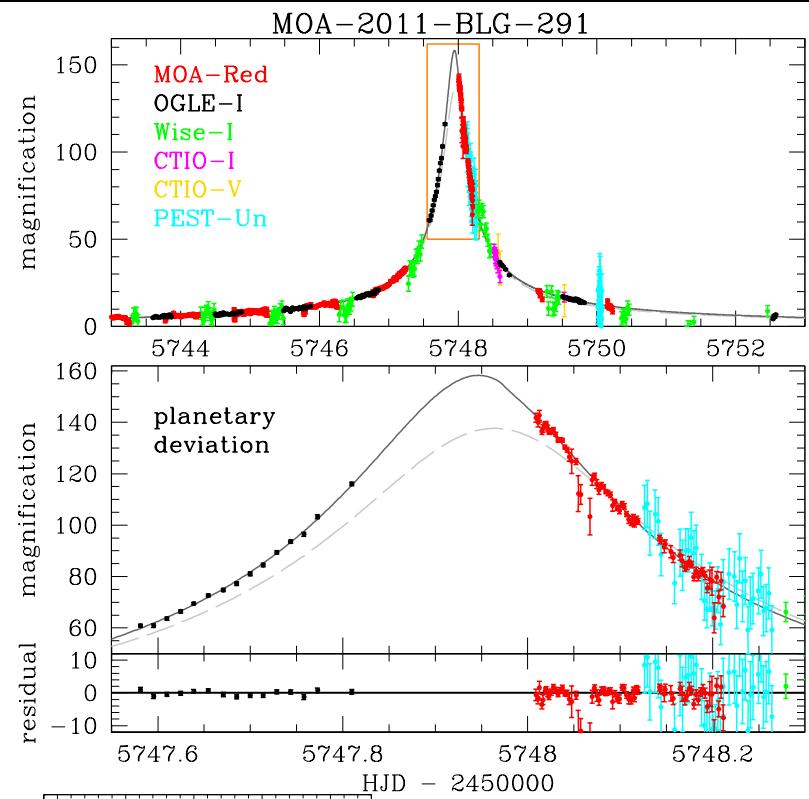
MOA-2010-BLG-353



$t_E = 11$ days
 $q = 1.3 \times 10^{-3}$
 $s = 1.5$

Rattenbury et al. in prep.

MOA-2011-BLG-291

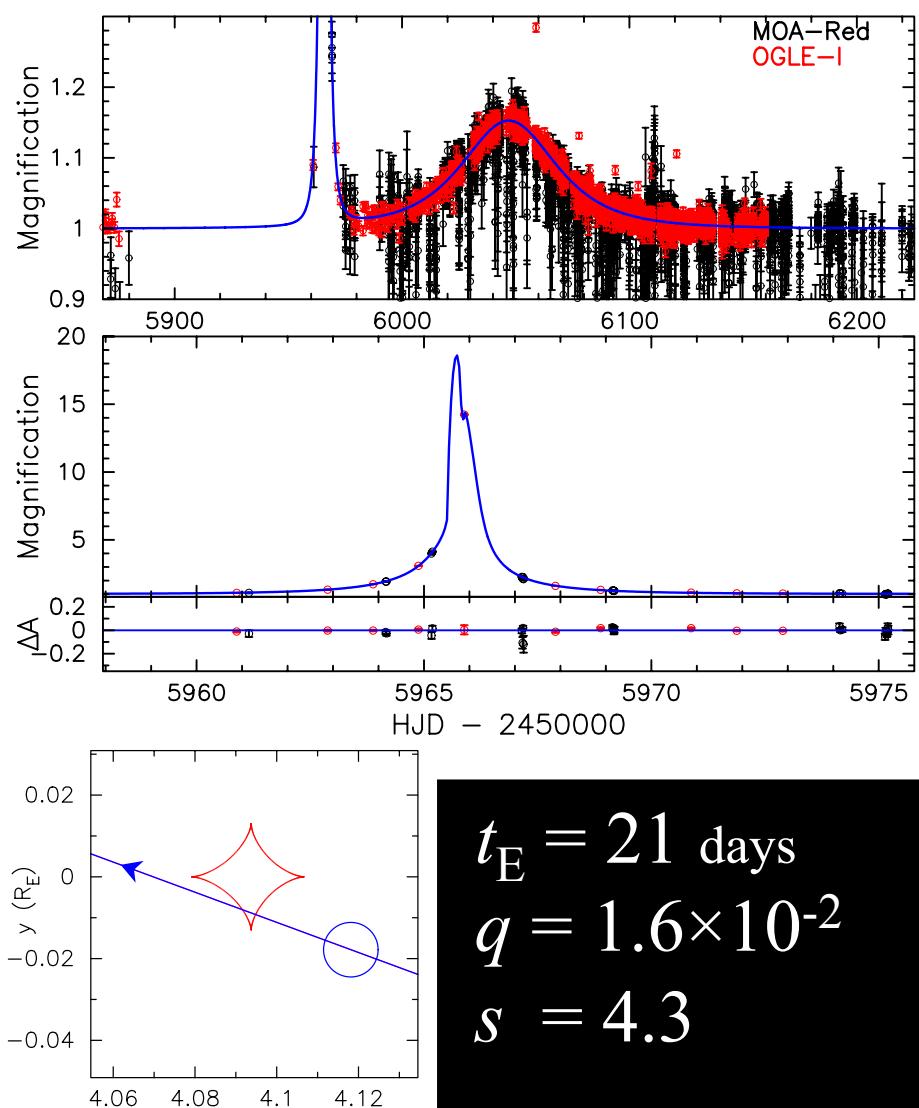


$t_E = 24$ days
 $q = 4.2 \times 10^{-4}$
 $s = 1.2$

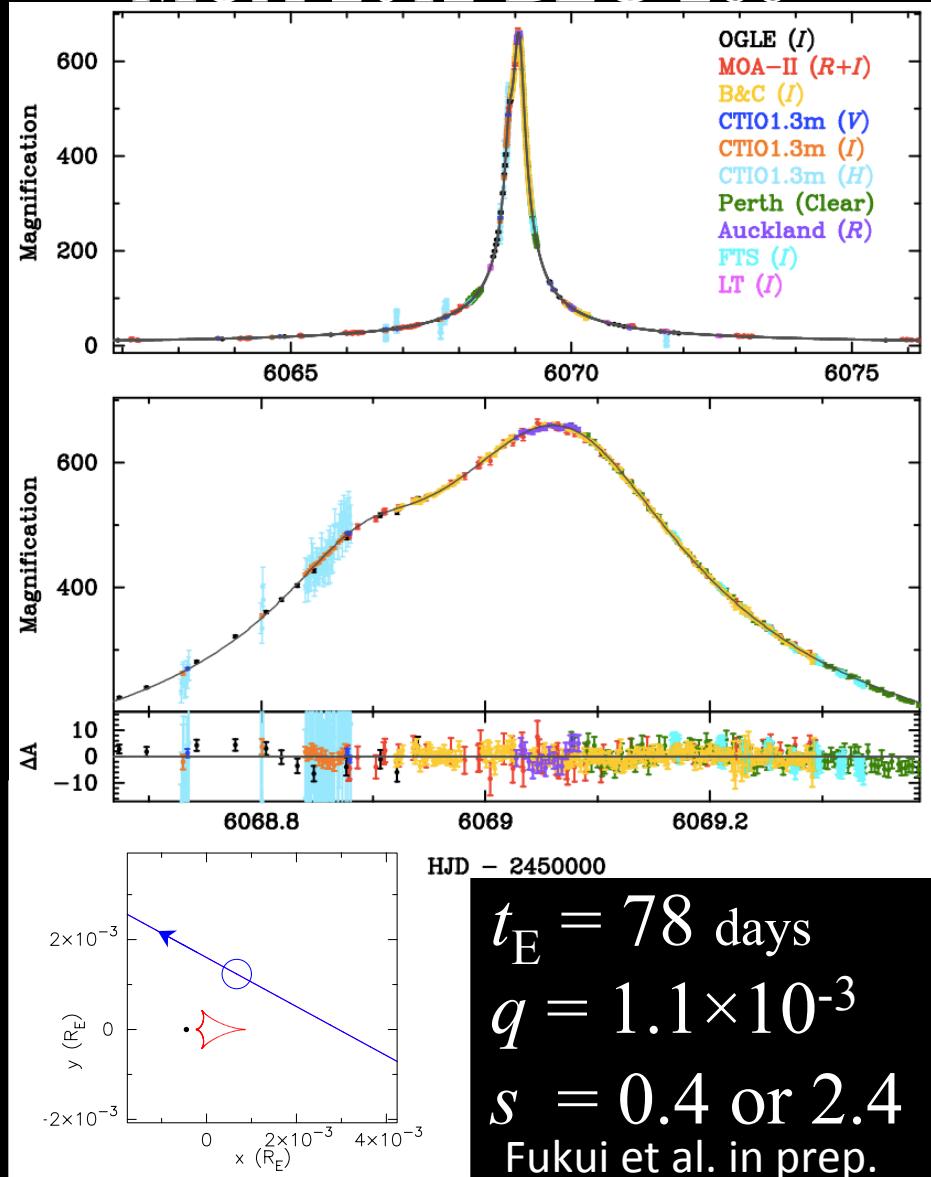
Bond et al. in prep.

Planets in 2012 Season

MOA-2012-BLG-006 /
OGLE-2012-BLG-0022

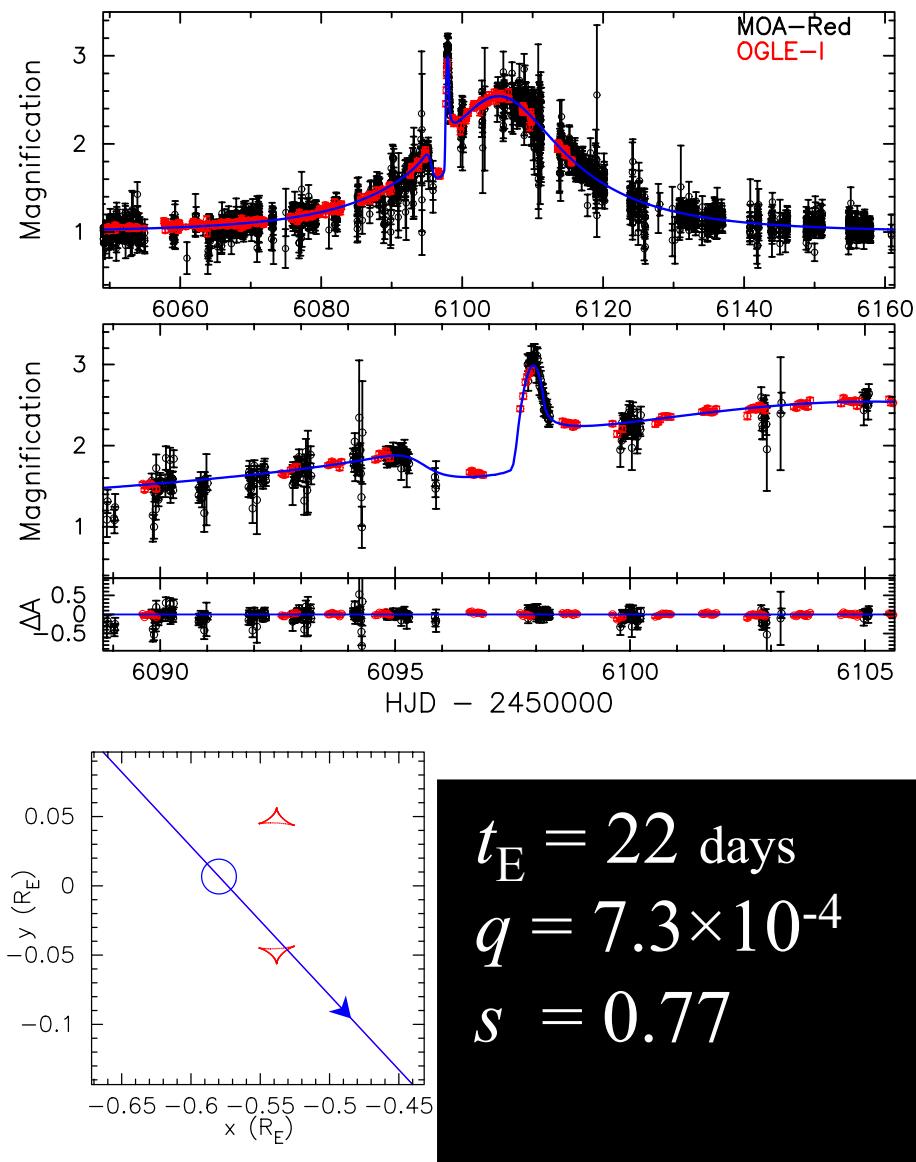


OGLE-2012-BLG-0563/
MOA-2012-BLG-288

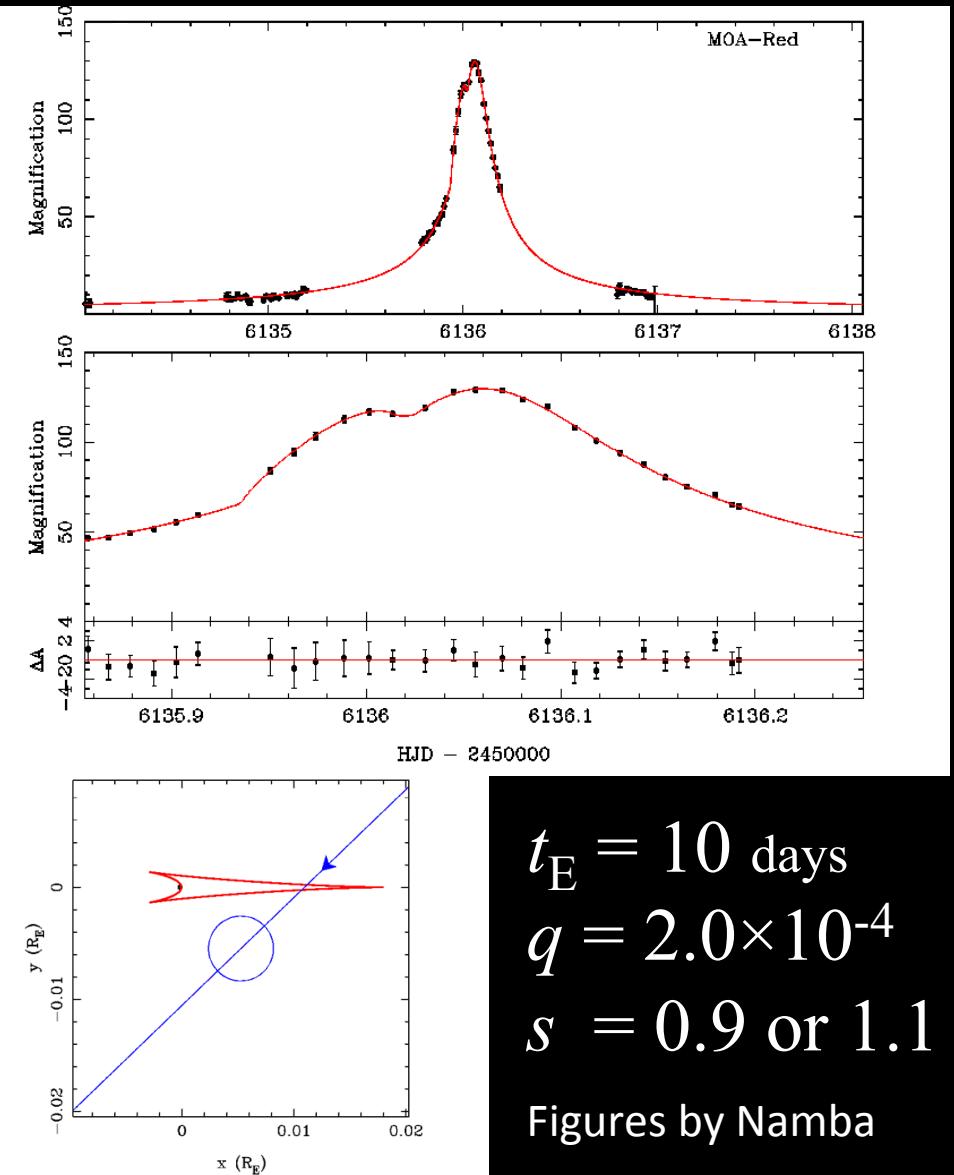


Planets in 2012 Season

MOA-2012-BLG-355



MOA-2012-BLG-505

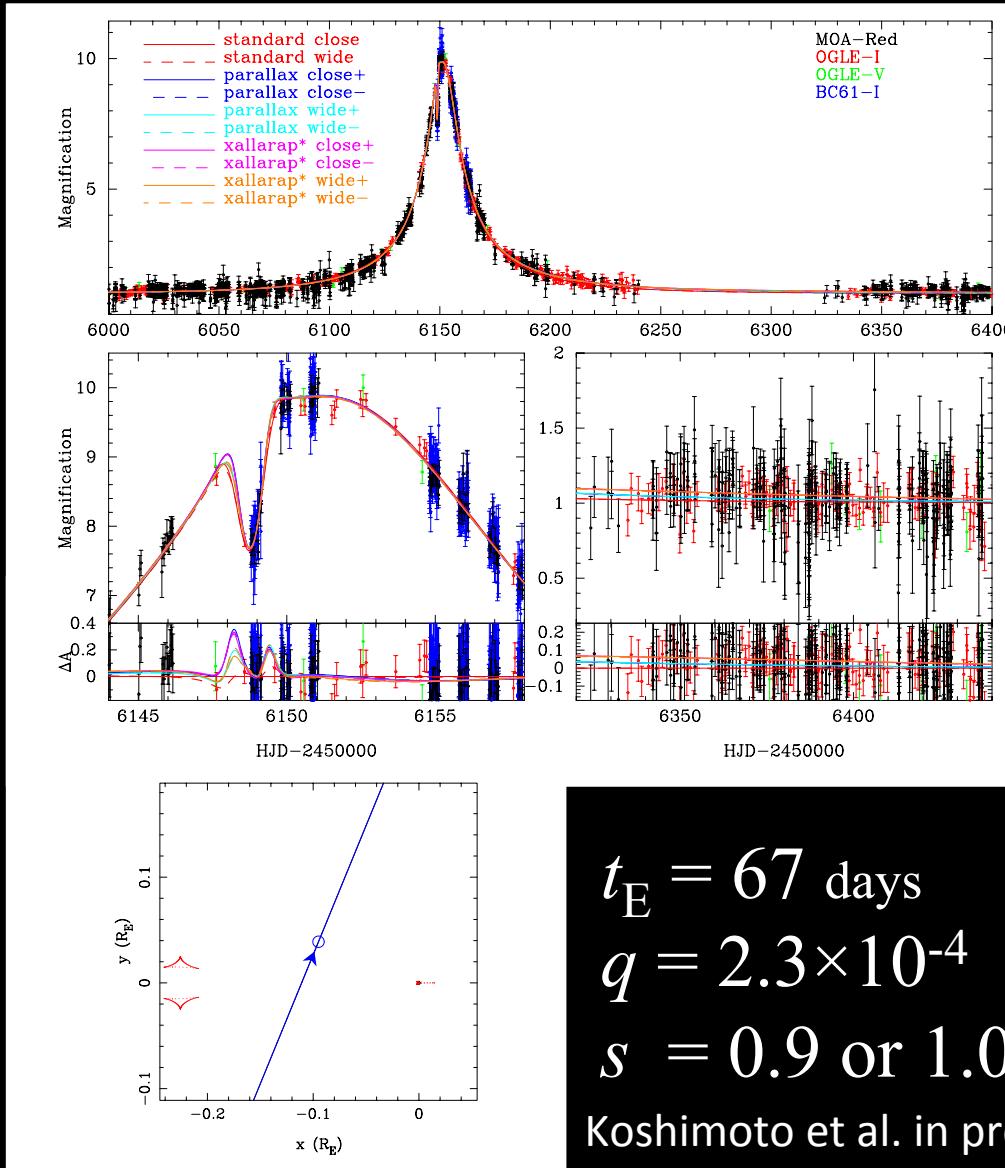


Planets in 2012 Season

OGLE-2012-BLG-0950 /

MOA-2012-BLG-527

Short Summary

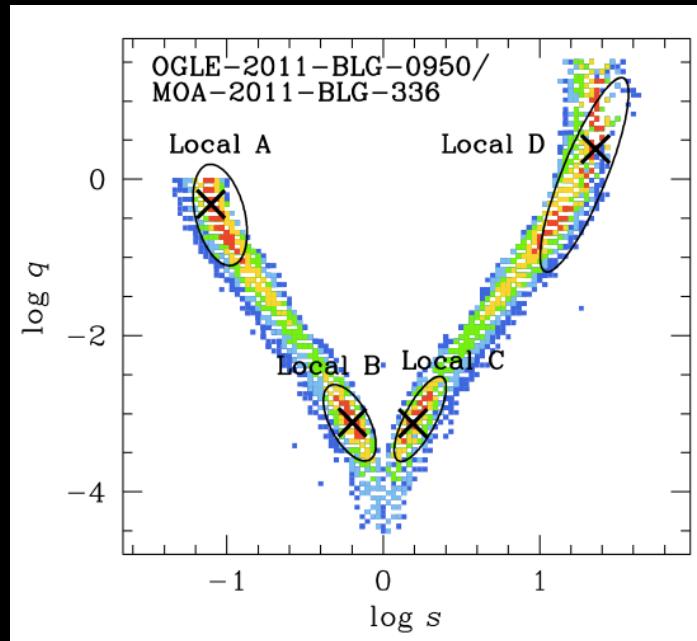
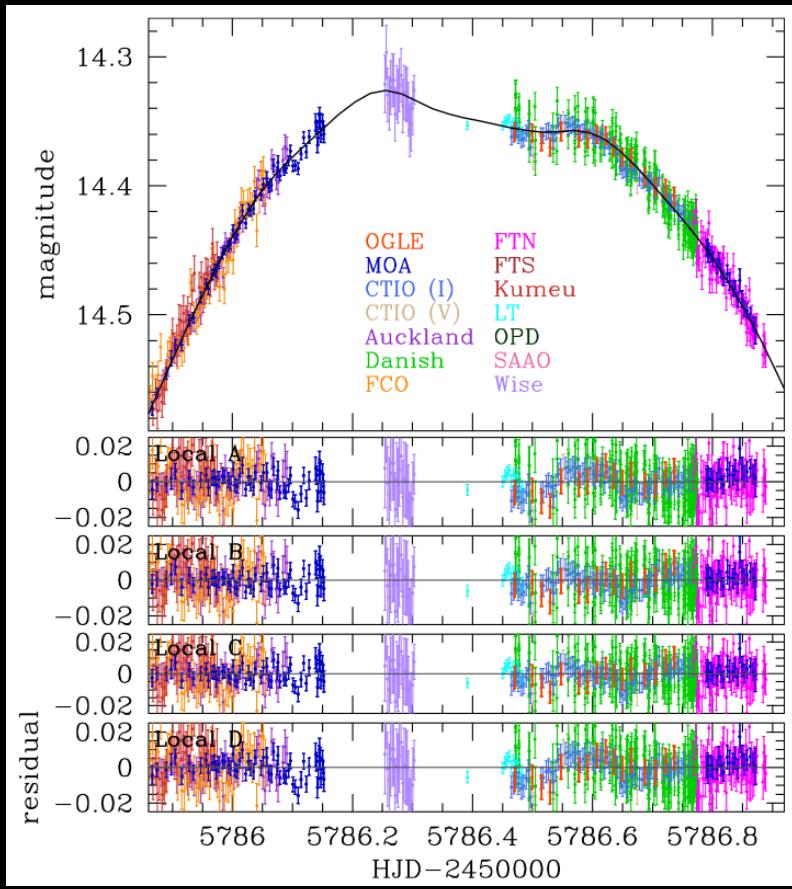


Event	Note
MB10353	Low-mag
MB11291	High-mag
MB12006/ OB120022	Low-mag, large s
OB120563/ MB12288	High-mag
MB12355	Low-mag, close to RR Lyrae
MB12505	High-mag, $t_E=10$
OB120950/ MB12527	Low-mag

3 Ambiguous (Planetary or Stellar Binary?)

- MB0789 / OB07141
- OB110950 / MB11336 (High-mag)
- MB12201 / OB120501

OB110950 / MB11336



our result: $\chi^2_{\text{SB}} - \chi^2_{\text{PL}} = 18$

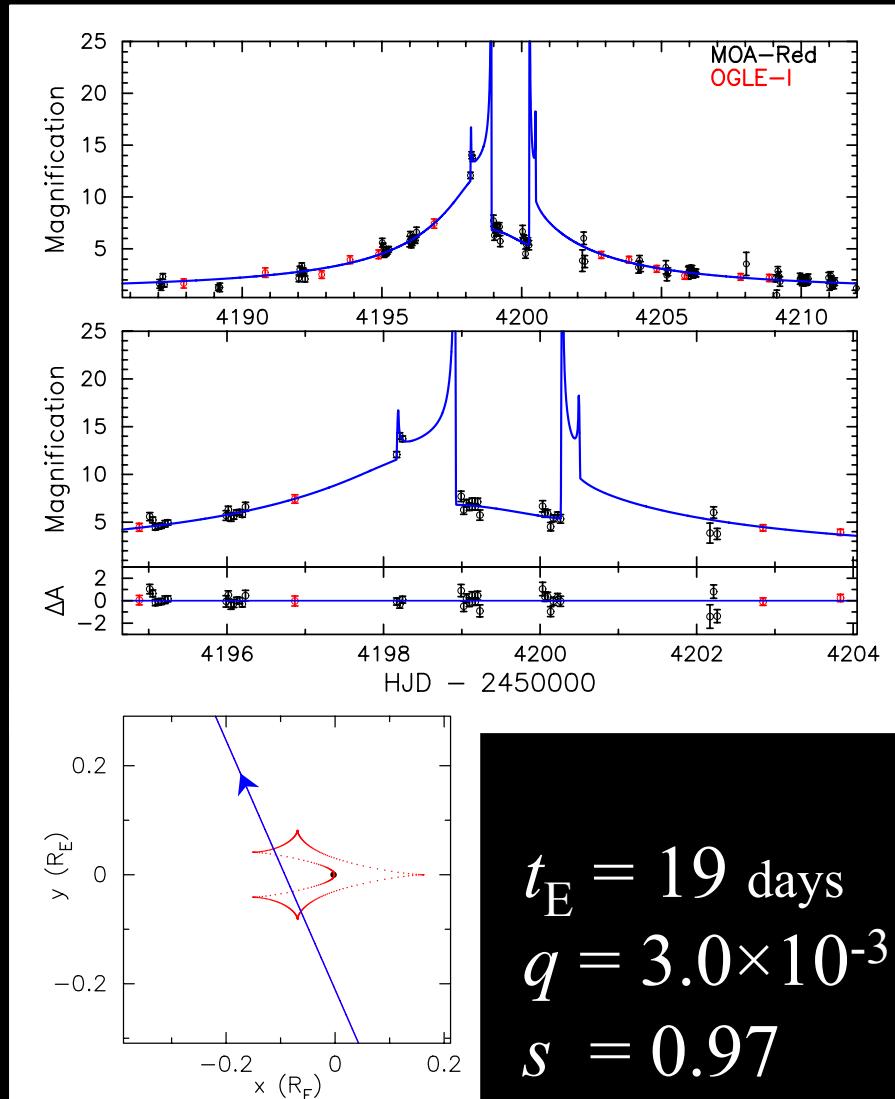
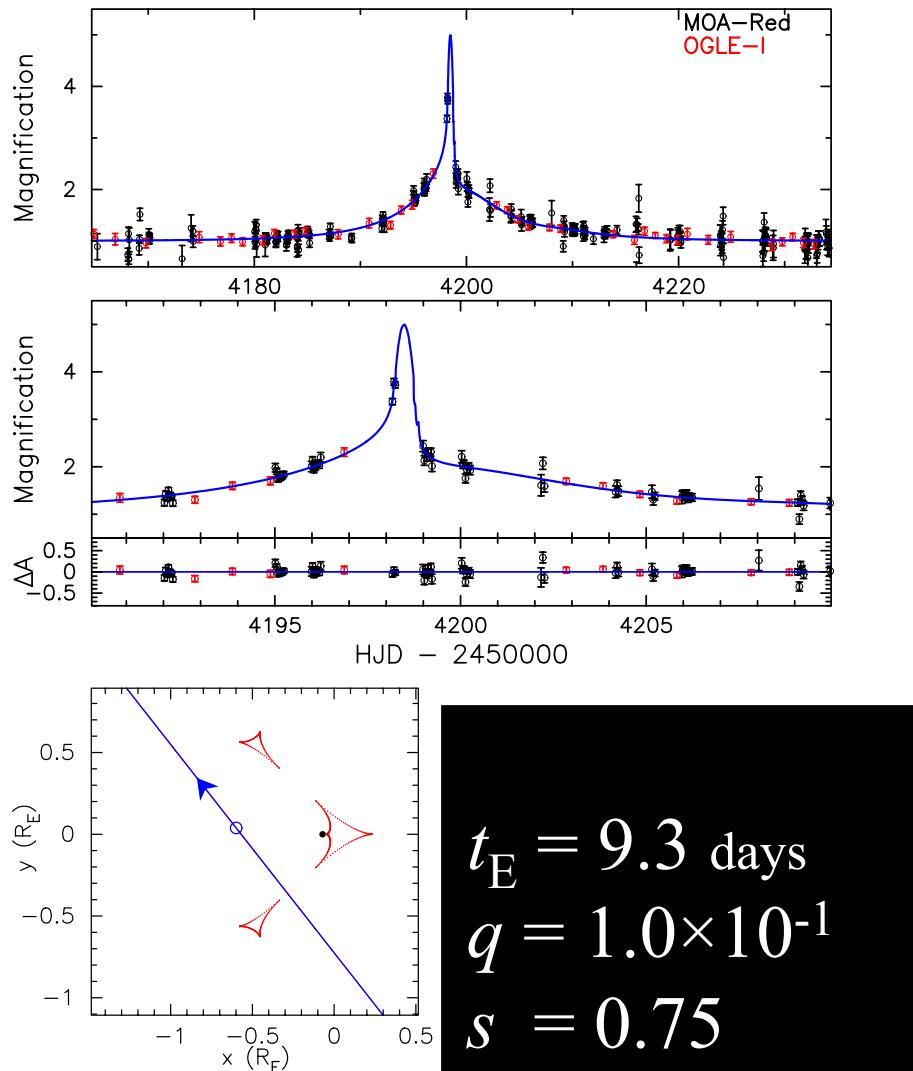
Choi et al. 2012

MB0789 / OB07141: Ambiguous Event

$$\chi^2_{\text{SB}} - \chi^2_{\text{PL}} = -3$$

Stellar Binary Model

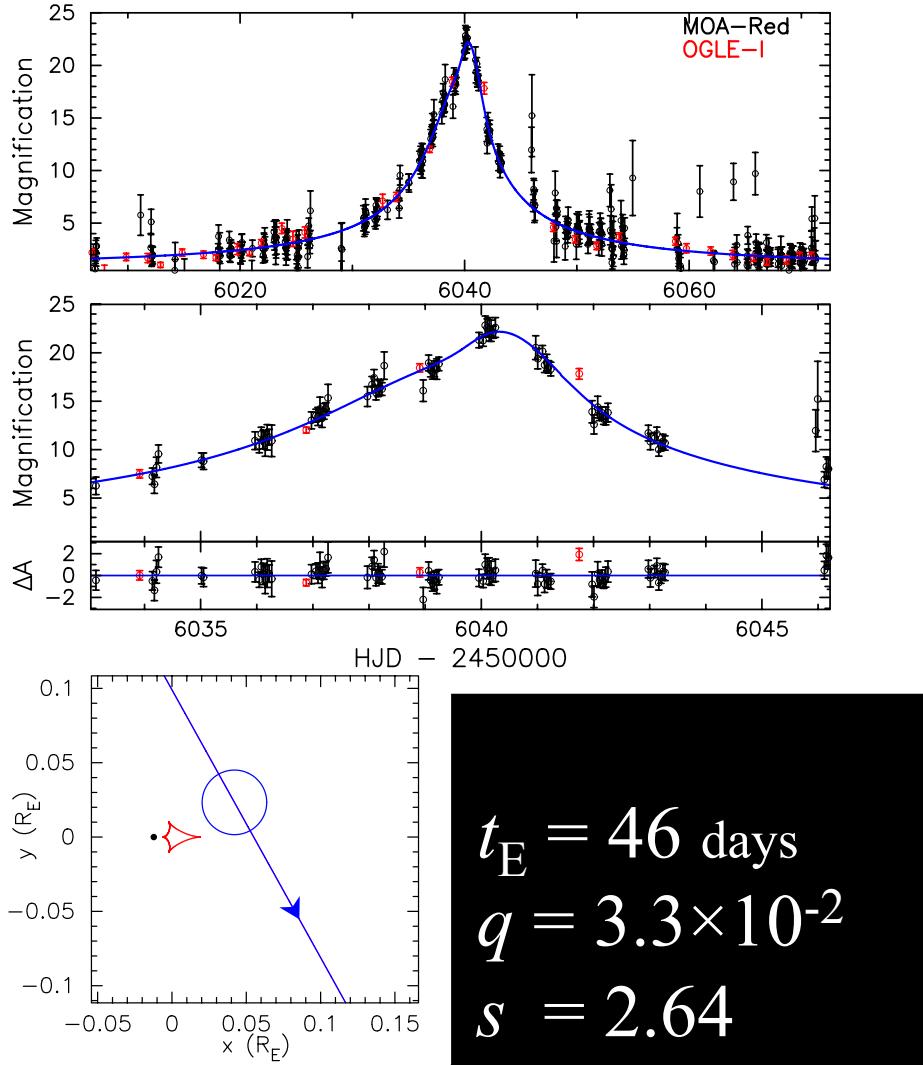
Planetary Model



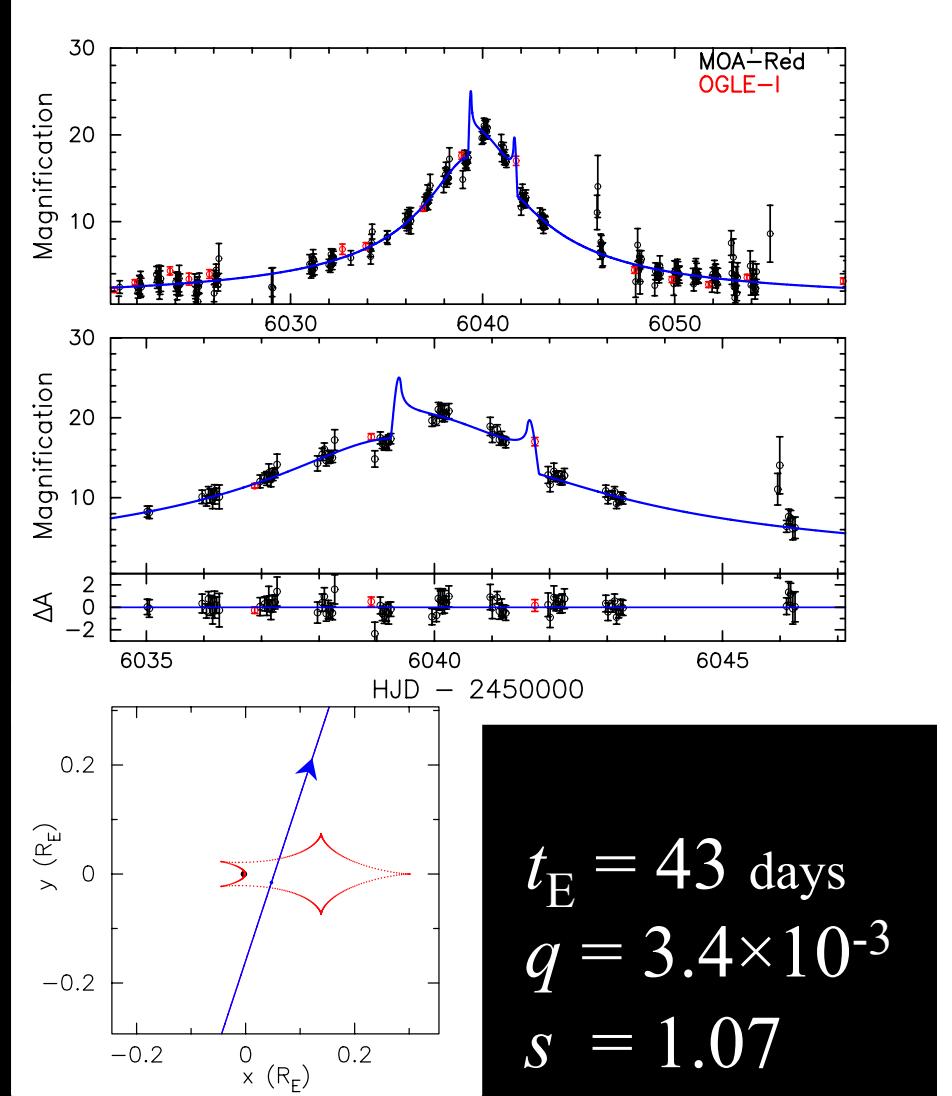
MB12201 / OB120501: Ambiguous Event

$$\chi^2_{\text{SB}} - \chi^2_{\text{PL}} = 8$$

Stellar Binary Model

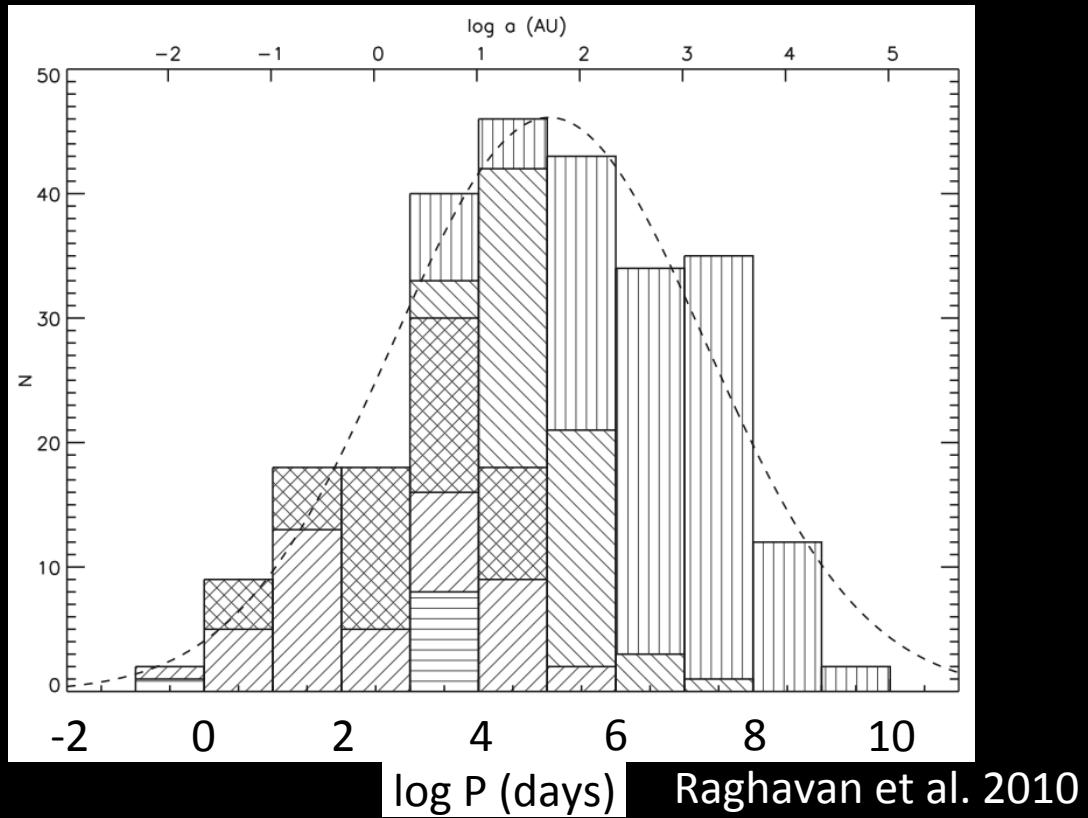


Planetary Model



Treating Ambiguous Events

1. $\Delta\chi^2$ between PL and SB model of light curve fitting
2. Prior probability of frequency for each companion
 - SB: Orbital period distribution (Raghavan et al. 2010),
Mass ratio function (Duchêne & Kraus 2013)
 - PL: Our mass ratio function



of planets
MB0789: 0.7
MB11336: 0.9
MB12201: 0.9

Detection Efficiency, $\varepsilon(\log s, \log q)$

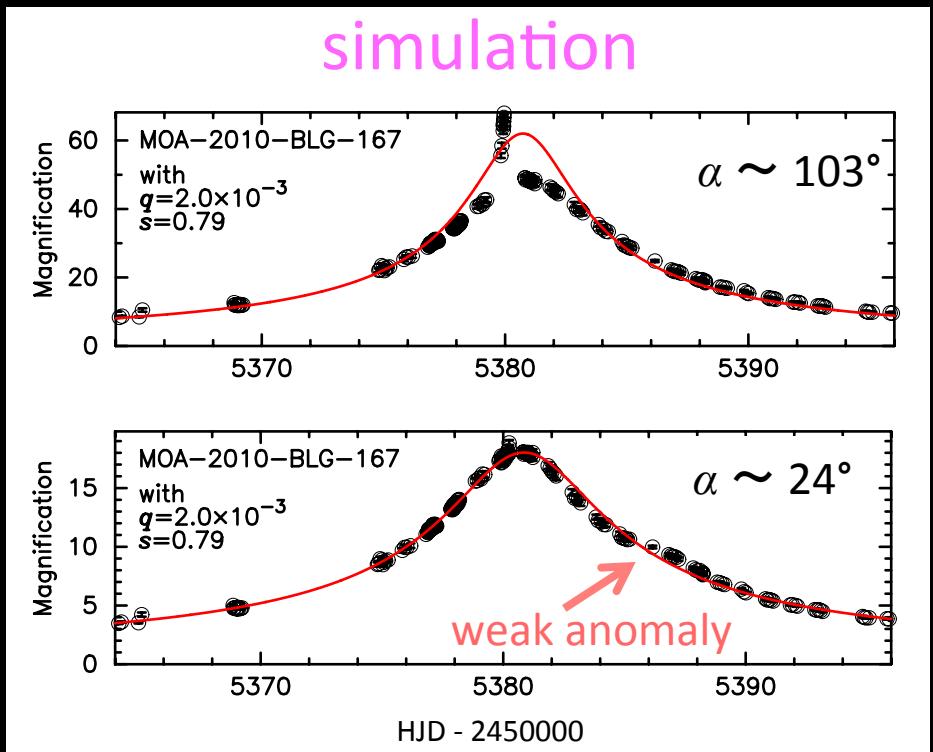
- q : mass ratio
- s : separation
- α : angle from the axis
- Data quality
- ρ : finite source effect

$$\rho = \theta_*/(t_E \mu_{\text{rel}})$$

θ_* : angular source star radius

$$\mu_{\text{rel}} = \langle \mu_{\text{rel}} \rangle = 5.2 \text{ mas/yr}$$

(Rhee+2000, Holtzman+ 1998,
Rattenbury+ 2007,
Kervella & Fouqué 2008,)



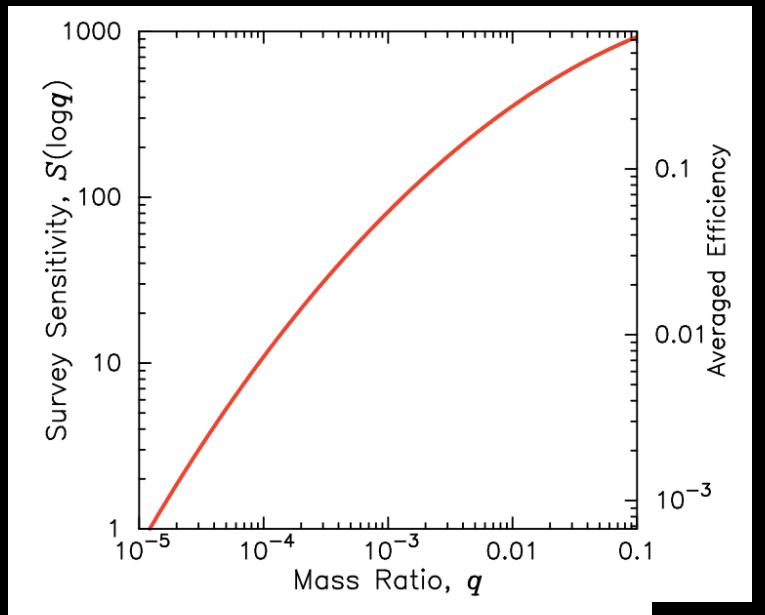
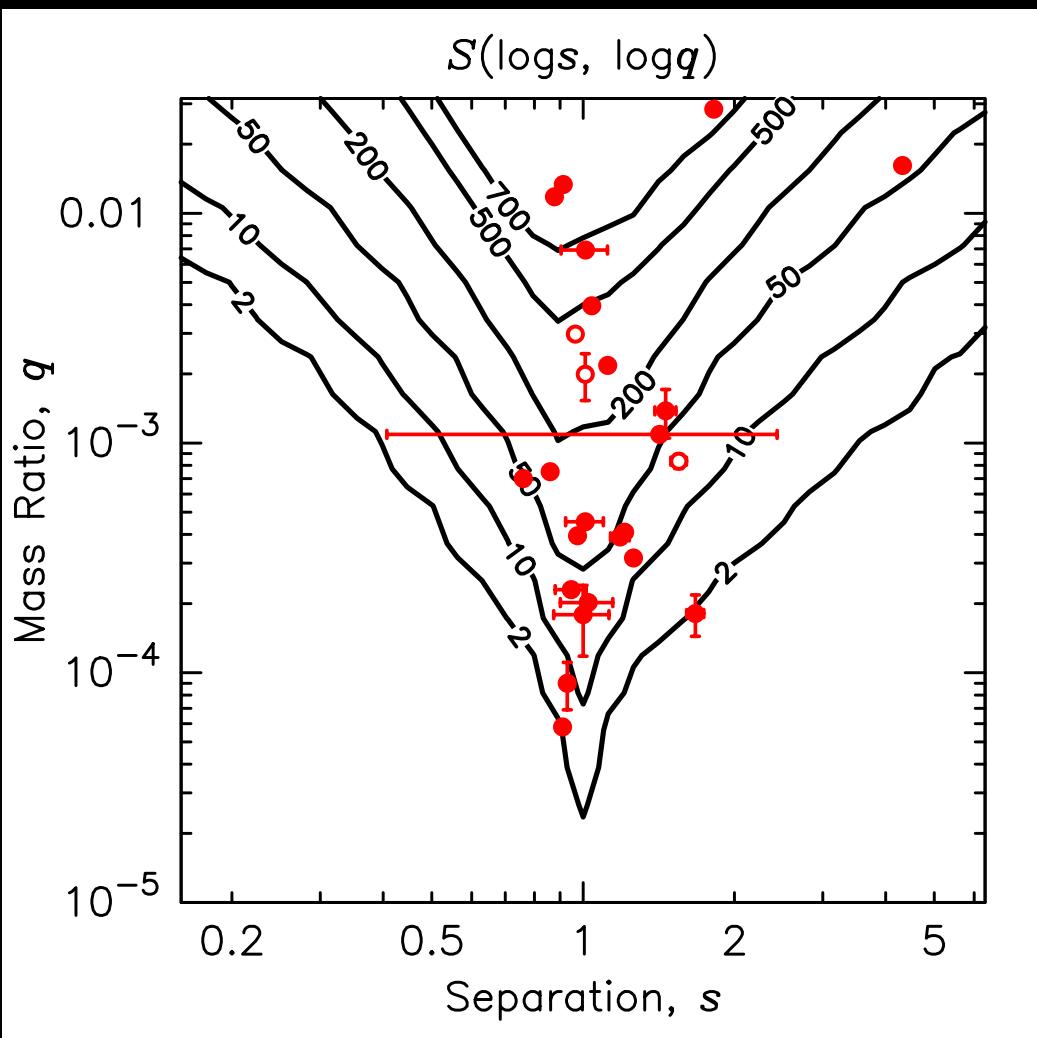
Detection:

$$\Delta\chi^2 = \chi^2_{\text{Single}} - \chi^2_{\text{Binary}} > 100$$

$\varepsilon(\log s, \log q)$:

Fraction of detections
within $0 < \alpha < 2\pi$

Detection Efficiency on s - q Plane



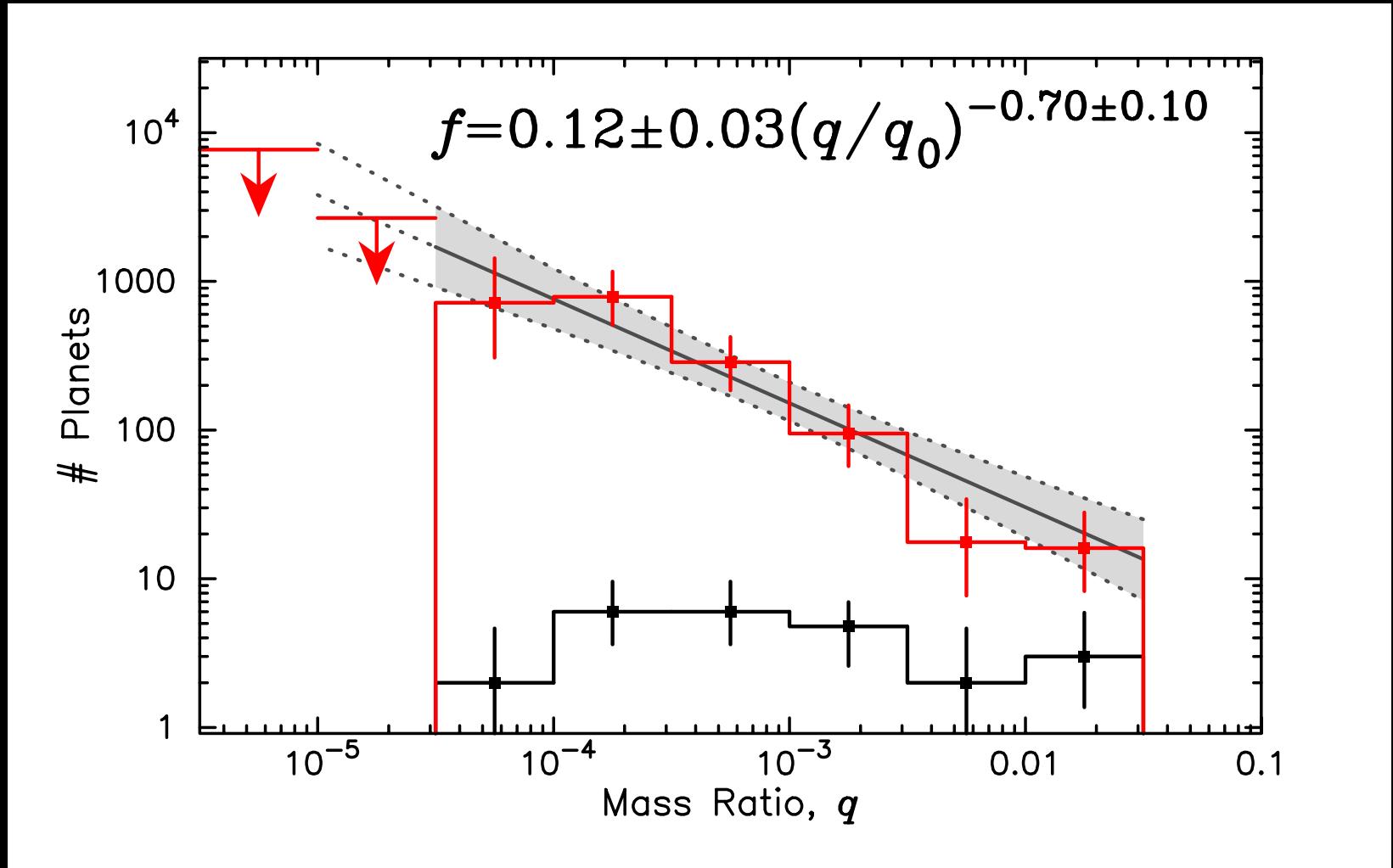
$$f \equiv \frac{dN}{d \log s \, d \log q} = A \left(\frac{q}{q_0} \right)^n$$

$$q_0 = 10^{-3}$$

$$L(A, n) = -N_{\text{exp}} + \sum_i^{N_{\text{obs}}} \ln f(q_i) S(\log q_i)$$

$$N_{\text{exp}} = \int_{q_-}^{q_+} dq f(q) S(\log q)$$

Planet Frequency with Mass Ratio

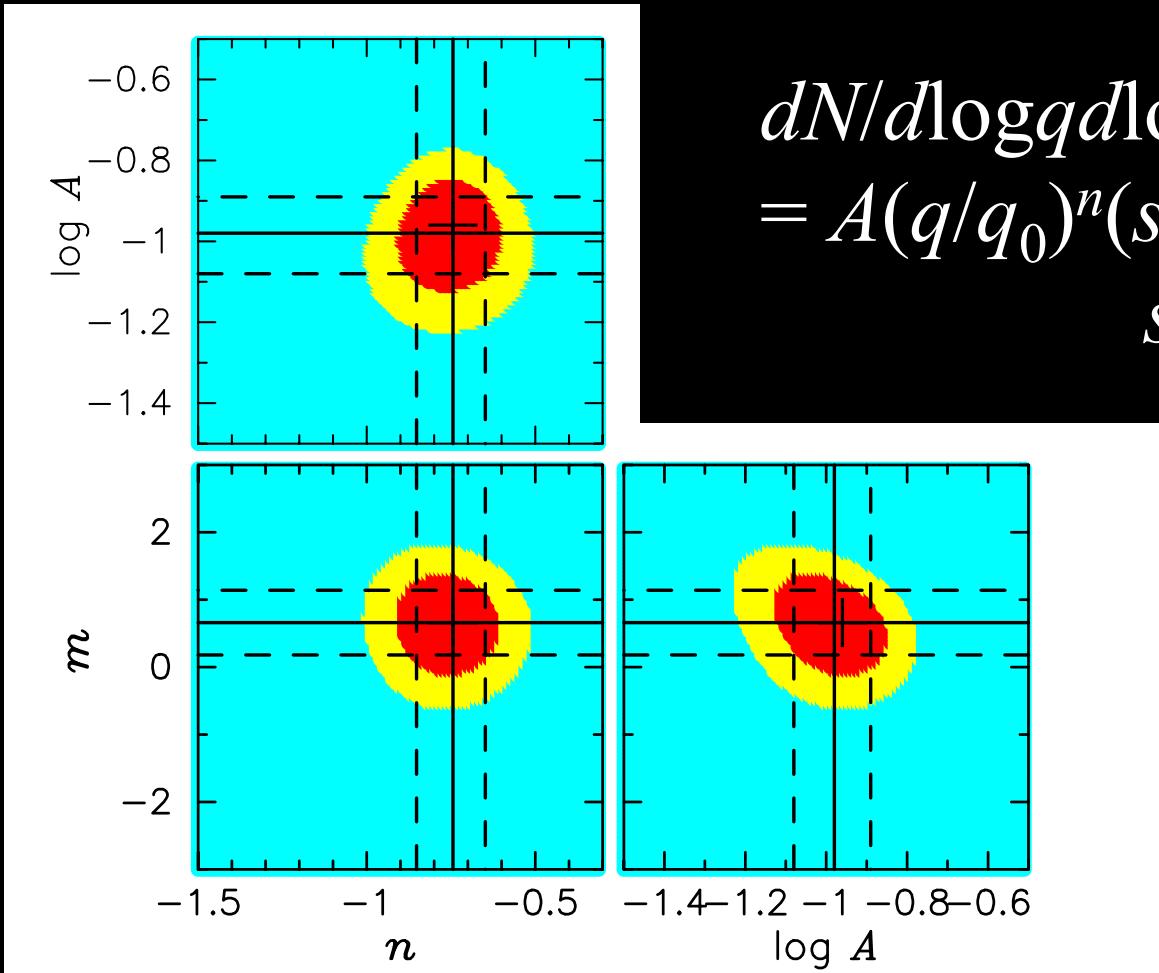


Cf. Sumi et al. 2010 : $f \propto (q/q_0)^{-0.68 \pm 0.20}$

Gould et al. 2010 : $N = 0.36 \pm 0.15$ @ $q = 5 \times 10^{-4}$

this work : $N = 0.20 \pm 0.06$ @ $q = 5 \times 10^{-4}$

Planet Frequency with q and s



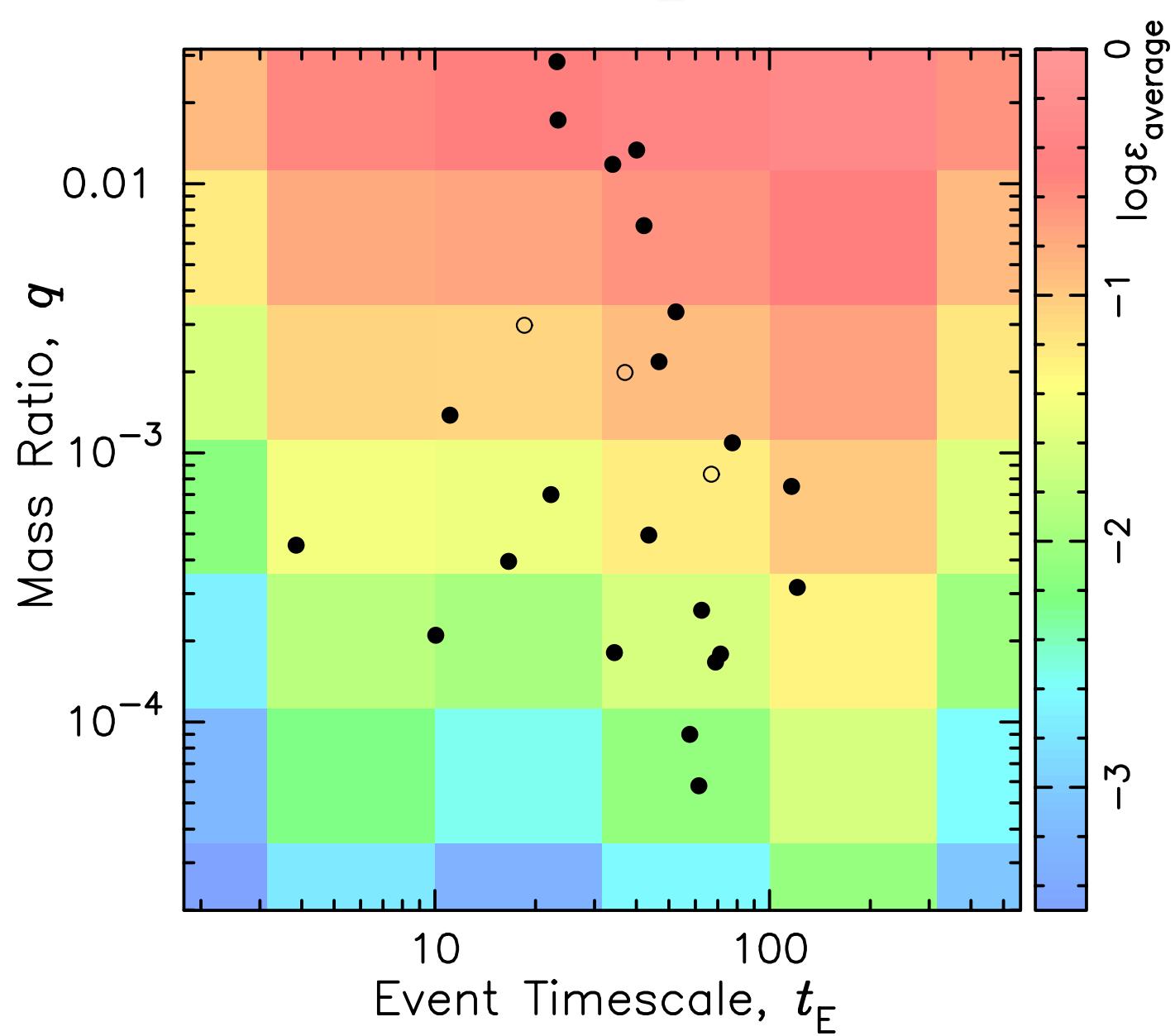
$$\begin{aligned} dN/d\log q d\log s \\ = A(q/q_0)^n (s/s_0)^m \\ s_0 = 1.0 \end{aligned}$$

preliminary

$$F = 0.10 \pm 0.02 (q/q_0)^{-0.74 \pm 0.10} (s/s_0)^{0.66 \pm 0.48}$$

Cf. Cumming et al. 2008: $dN = CM^\alpha P^\beta d\ln M d\ln P$, $\beta = 0.26 \pm 0.10$

Detection Efficiency on t_E - q plane



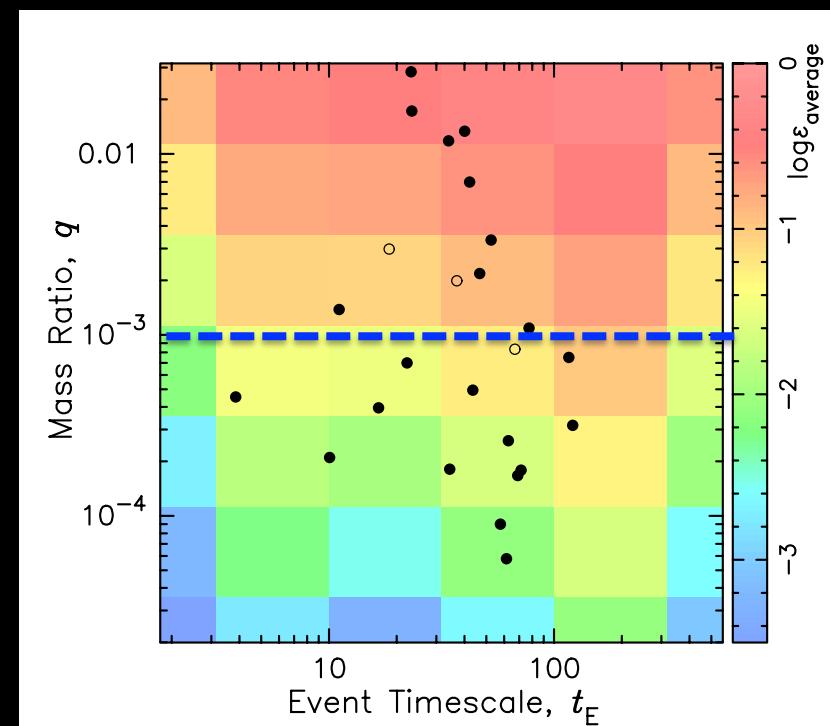
Planet Frequency with Event Time Scale

$$F = C(t_E/t_{E0})^\gamma$$

$$t_{E0} = 20 \text{ days}$$

if $\gamma > 0$, planets favor

- Massive stars
- Nearby disk stars



Planet Frequency with Event Time Scale

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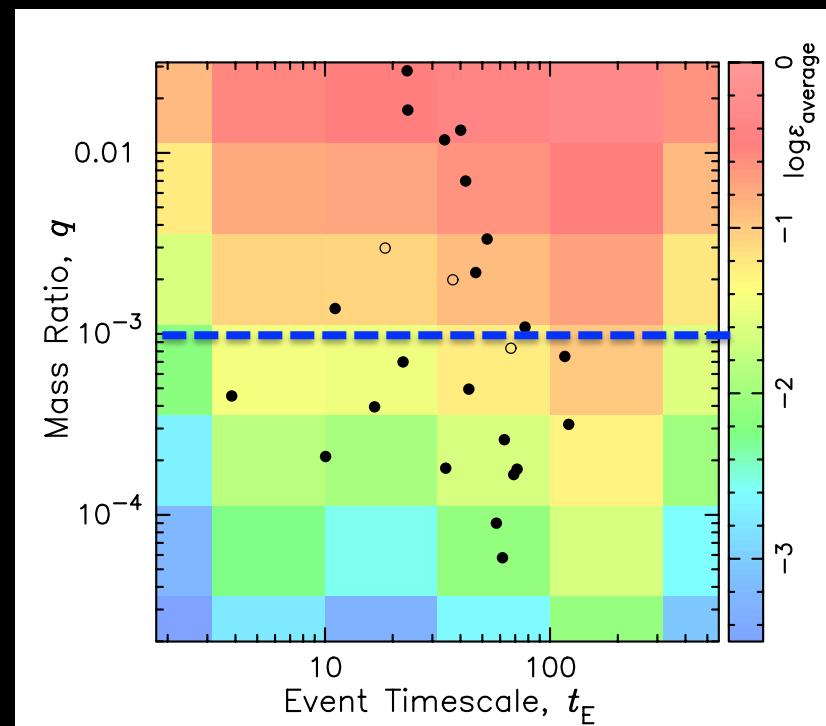
- Massive stars
- Nearby disk stars

For the planets with $q > 0.001$

$$\gamma = 0.15 \pm 0.45$$

For the planets with $q < 0.001$

$$\gamma = 0.15 \pm 0.30$$



preliminary

Summary

From MOA survey in 2007-2012, 1291 single lens,
22 planetary and 3 ambiguous events are used

- $F = 0.12 \pm 0.03 (q/q_0)^{-0.70 \pm 0.10}; q_0 = 10^{-3}$
- $F = 0.10 \pm 0.02 (q/q_0)^{-0.74 \pm 0.10} (s/s_0)^{0.66 \pm 0.48}; s_0 = 1.0$
- Uncertainty in the slope and normalization
are twice smaller than previous works' values
- $F \propto (t_E/t_{E0})^\gamma$; γ is consistent with 0; $t_{E0}=20$ days

Statistical exoplanet analysis of MOA-II survey
data leads a way for the coming survey era